

[Time : 2.30 Hours]

[Marks: 60]

Please check whether you have got the right question paper.

NB;

1. All questions are compulsory.
2. Figures to the right indicate full marks.
3. Use of non-programmable calculator is allowed.

Useful constants:

$$c = 2.998 \times 10^8 \text{ ms}^{-1}$$

$$R = 8.314 \text{ JK}^{-1} \text{ mol}^{-1}$$

$$h = 6.626 \times 10^{-34} \text{ Js}$$

$$N_A = 6.022 \times 10^{23} \text{ mol}^{-1}$$

$$e = 1.602 \times 10^{-19} \text{ C}$$

$$J = 6.24 \times 10^{18} \text{ eV}$$

$$1 \text{ atm} = 1.013 \times 10^5 \text{ Nm}^{-2}$$

$$1 \text{ eV} = 8.06 \times 10^3 \text{ cm}^{-1}$$

$$1 \text{ amu} = 1.66 \times 10^{-27} \text{ kg}$$

Atomic mass of H = 1, C = 12, N = 14, O = 16

Q.1 a Attempt any two of the following :

- (i) Show that the pressure is a state function for an ideal gas obeying the equation of state 4

$$(P + \frac{a}{V^2})(V - b) = RT$$

- (ii) State the third law of thermodynamics. Give its application. Why molecules like CO and N₂O have positive value of entropy at zero Kelvin? 4

- (iii) Define Joule-Thomson coefficient. Give its significance. 'Ideal gases do not show Joule-Thomson effect.' Explain. 4

- (iv) Write the expression for entropy changes in the following phase transitions 4
- i) Melting
 - ii) Vapourisation
 - iii) Sublimation
 - iv) Allotropic transformation

(b) Attempt any one of the following:

- (i) A function ϕ is defined as $\phi(x,y) = x^2y^3 + x$. Write its partial derivatives and total differential. Test whether $d\phi$ is an exact differential or not. 4
- (ii) A piece of alloy weighing 2 kg and at a temperature of 500°C is placed in 4 kg of water at 300K. If the heat capacity of water is $4.184 \text{ JK}^{-1} \text{ g}^{-1}$ and that of alloy is $22 \text{ JK}^{-1} \text{ g}^{-1}$. Calculate the entropy change. 4

Q.2 a Attempt any two of the following :

- (i) What are the characteristics of a wave function to be acceptable? Show that the normalised wave function of a particle in a one dimensional box is given by, 4

$$\varphi_{(n)} = \left(\frac{2}{a}\right)^{1/2} \sin\left(\frac{n\pi x}{a}\right)$$

- (ii) Derive the Hermite's differential from the relation 4

$$\frac{d^2\psi}{dy^2} + \left(\frac{\alpha}{\beta} - y^2\right)\psi = 0$$
- (iii) Obtain an expression for energy of a particle in one dimensional box of length 'a'. 4
- (iv) State the postulates of quantum mechanics. 4
- (b) Attempt **any one** of the following:
- (i) The Hermite polynomials are derived from the generating function 4

$$H_n(y) = (-1)^n e^{y^2} \frac{d^n}{dy^n} (e^{-y^2})$$

 Calculate the polynomial for n=1 and n=3
- (ii) Calculate the lowest kinetic energy of an electron in a three dimensional box of dimensions 0.001pm, 0.0015pm and 0.002pm. 4

Q.3a Attempt any two of the following :

- (i) Write the reactions for thermal decomposition of acetaldehyde. Using steady state approximation show that the rate of formation of methane is given by 4

$$\frac{d[\text{CH}_4]}{dt} = k [\text{CH}_3\text{CHO}]^{3/2}$$
- (ii) H₂ reacts with Br₂ to give HBr according to the reaction 4

$$\text{H}_2 + \text{Br}_2 \xrightarrow{h\nu} 2\text{HBr}$$
 Using the chain reaction mechanism, obtain the rate equation for the above thermal reaction.
- (iii) Describe the effect of pressure and temperature on the rate of an explosion reaction with the help of a suitable example. 4
- (iv) Give a brief account of the Lindeman-Hinshelwood theory of unimolecular reactions in gas phase. 4
- (b) Attempt **any one** of the following:
- (i) The rate of formation of C in the reaction, 4

$$2\text{A} + \text{B} \rightarrow 2\text{C} + 3\text{D}$$
 is 1 mol L⁻¹ s⁻¹. State the reaction rate and the rates of formation or consumption of A, B and D
- (ii) Consider the following consecutive reaction 4

$$\text{R}_1 \xrightarrow{k_1} \text{R}_2 \xrightarrow{k_2} \text{R}_3$$
 Where k_1 and k_2 are the rate constants for a first order reaction. If the initial concentration of R₁ is 1 M and $k_1:k_2$ 1.0:0.15. Calculate the concentration of each species after 10 seconds. Given $k_1 = 4 \times 10^{-2} \text{ min}^{-1}$.

Q.4a Attempt any two of the following :

- (i) Derive an equation for the Debye -Huckel limiting law. 4
- (ii) State Debye-Huckel-Onsager equation and discuss its validity for aqueous solutions. 4
- (iii) With the help of diagram explain the working of solid oxide fuel cell. 4
- (iv) Explain Deby-Falkenhagen and wien effect. 4

(b) Attempt any **one** of the following:

- (i) Calculate the mean activity coefficient of (i) NaCl at a molality of 0.01 (ii) 4
 Na₂SO₄ at a molality of 0.001 in aqueous solution at 25°C. ((
- Given :A for water at 25° C is 0.509)
- (ii) Calculate the resting membrane potential for a living cell for the following 4
 concentrations of Na⁺ and K⁺ at 298K.
 Intra cellular concentration of K⁺ = 410mM Na⁺ = 40mM
 Extra cellular concentration of K⁺ = 16mM Na⁺ = 380mM
 (given : 2.303RT/ F = 60 at 298K)

Q.5 Attempt any four of the following :

- a Explain the determination of absolute entropy with the help of heat capacity 3
 concept.
- b Derive the relation: 3

$$\left(\frac{\partial P}{\partial T} \right)_V = \left(\frac{\partial S}{\partial V} \right)_T$$
- c State Heisenberg's uncertainty principle. An electron moves in the first orbit 3
 with a speed of $2 \times 10^6 \text{ ms}^{-1}$. If its momentum is measured with an accuracy of
 1 %, what is uncertainty of position?
- d Give an expression for allowed energy levels of linear harmonic oscillator. 3
 Comment on spacing of energy levels. What is zero point energy?
- e Explain consecutive reactions with examples. 3
- f Give a brief account of Rice-Ramsperger-Kassel-Marcus theory. 3
- g Write a note on enzyme-catalysed oxidation of styrene. 3
- h State any three applications of Alkaline fuel cell. 3