

- N.B. :** (1) All questions are compulsory.
 (2) Figures to the right indicate full marks.
 (3) Uses of non-programmable scientific calculator is allowed.

Useful constants

$$c = 2.998 \times 10^8 \text{ ms}^{-1}$$

$$e = 1.602 \times 10^{-19} \text{ C}$$

$$R = 8.314 \text{ JK}^{-1} \text{ mol}^{-1}$$

$$k = 1.3811 \times 10^{-23} \text{ JK}^{-1}$$

$$h = 6.626 \times 10^{-34} \text{ Js}$$

$$1 \text{ J} = 6.24 \times 10^{18} \text{ eV}$$

$$m_e = 9.110 \times 10^{-31} \text{ kg}$$

$$1 \text{ eV} = 8.06 \times 10^3 \text{ cm}^{-1}$$

$$N_A = 6.023 \times 10^{23} \text{ mol}^{-1}$$

$$1 \text{ amu} = 1.66 \times 10^{-27} \text{ kg}$$

1. (A) Attempt any two of the following :
- (a) Write the Schrodinger wave equation for a particle in one dimensional box and obtain an energy expression for the same. Why is the value for quantum number $n = 0$ not permitted? 4
- (b) Formulate the Schrodinger wave equation for a particle of mass 'm' and wavelength ' λ ' having motion in three dimensions. 4
- (c) What is the condition for orthogonality of wave functions? Show that two normalised wave functions ψ_1 and ψ_2 are orthogonal to each other. 4
- (d) Show that the probability of finding a free particle in limitless space at all points is the same. 4
- (B) Attempt any one of the following :
- (a) The Hermite polynomials are derived from the 'generating function'. 4
- $$H_n(y) = (-1)^n e^{y^2} \frac{d^n (e^{-y^2})}{dy^n}$$
- Calculate the polynomial for $n = 1$ and $n = 2$. 4
- (b) For a particle of mass 'm' moving in a cubical box of side 'a', calculate the degeneracy of the level corresponding to the energy
- (i) $E = \frac{18h^2}{8ma^2}$ (ii) $E = \frac{21h^2}{8ma^2}$

2. (A) Attempt any two of the following :

- (a) Solve the following partial differential equation by separating the two variables to obtain two ordinary differential equations containing one variable each. 4

$$\frac{\partial^2 \psi}{\partial \theta^2} + \frac{\cos \theta}{\sin \theta} \frac{\partial \psi}{\partial \theta} + \frac{1}{\sin^2 \theta} \frac{\partial^2 \psi}{\partial \phi^2} + \frac{8\pi^2 m r^2}{h^2} E \psi = 0$$

- (b) Explain why a two electron system can also be called "an independent electron model". 4
- (c) On the basis of angular probability distribution curves, explain the shapes of s-orbital. 4
- (d) With respect to hydrogen like atom, answer the following : 4
- (i) Write the Hamiltonian operator for it and identify the terms involved.
- (ii) Mathematically express the "coordinates of the centre of mass" and relative coordinates of the system.

(B) Attempt any one of the following :

- (a) Calculate the values for the first three rotational energy levels of a rigid rotor, whose moment of inertia is $1.457 \times 10^{-46} \text{kgm}^2$. 4
- (b) Calculate the most probable distance of an electron from the nucleus in ground state of hydrogen atom. The normalised ground state 4

function is $\psi_{1s} = \frac{1}{\sqrt{\pi} a_0^{3/2}} e^{-\frac{r}{a_0}}$

3. (A) Attempt any two of the following :

- (a) What is collision number? Explain why the observed rate of bimolecular polymerisation of ethylene is much lower than predicted by collision theory. 4
- (b) Explain the kinetics of free radical chain polymerisation. 4
- (c) Explain the mechanism of decomposition of ozone. 4
- (d) Give a brief account of Rice-Ramsperger - Kassel theory. 4

(B) Attempt any one of the following :

- (a) A bottle of milk stored at 30°C sours in 36 hours, stored in a refrigerator at 5°C sours after one week. Assuming the rate constant to be inversely related to the souring time, estimate the activation energy of a chemical reaction involved in souring process. 4

- (b) The molecular diameters of O₂ and H₂ gases are $3.39 \times 10^{-10}\text{m}$ and $2.47 \times 10^{-10}\text{m}$ respectively. Calculate the number of collisions in $\text{m}^{-3}\text{s}^{-1}$, when 1.0g of O₂ and 0.1 g of H₂ are mixed in one dm^3 flask at 300 K. 4
4. (A) Attempt any two of the following :
- (a) Derive an expression of parabolic rate law for kinetics of reactions in the solid state. 4
- (b) Derive an expression of the contracting area rate law for kinetics of reactions in the solid state. 4
- (c) Derive an expression to show the effect of dielectric constant on the rate of reaction between ions in solution. 4
- (d) Derive Hammett equation to show the effect of substituents on the reaction rates. 4
- (B) Attempt any one of the following :
- (a) Discuss the kinetics of enzyme inhibition by uncompetitive inhibition method. 4
- (b) Derive the Michaelis - Menten equation of enzyme catalysed reaction. 4
5. Attempt any four of the following :
- (A) With the help of suitable example, explain the terms eigen function and eigen value. 3
- (B) "Eigen values of Hermitian operator are real". Prove. 3
- (C) Write the expression for potential energy of hydrogen like system. Why is it characterised by spherically symmetric potential energy? 3
- (D) Name the four quantum numbers required to specify the state of an electron in an atom. Give their allowed values and significance in general. 3
- (E) Explain consecutive reactions with suitable examples. 3
- (F) Explain free radical mechanism of polymerisation of ethylene. 3
- (G) Explain how Lineweaver - Burk plot is used for analysing the rate data of enzyme catalysed reactions. 3
- (H) Write a note on factors affecting reactions in solids. 3
